



Accelerating and improving  
quantum chemistry and  
dynamics with  
artificial intelligence

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# Group & Acknowledgements

Hiring post-docs, PhD & MSc students!



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嘉庚创新实验室  
TAN KAH KEE INNOVATION LABORATORY



*Ca. 2 mln people on Xiamen Island*

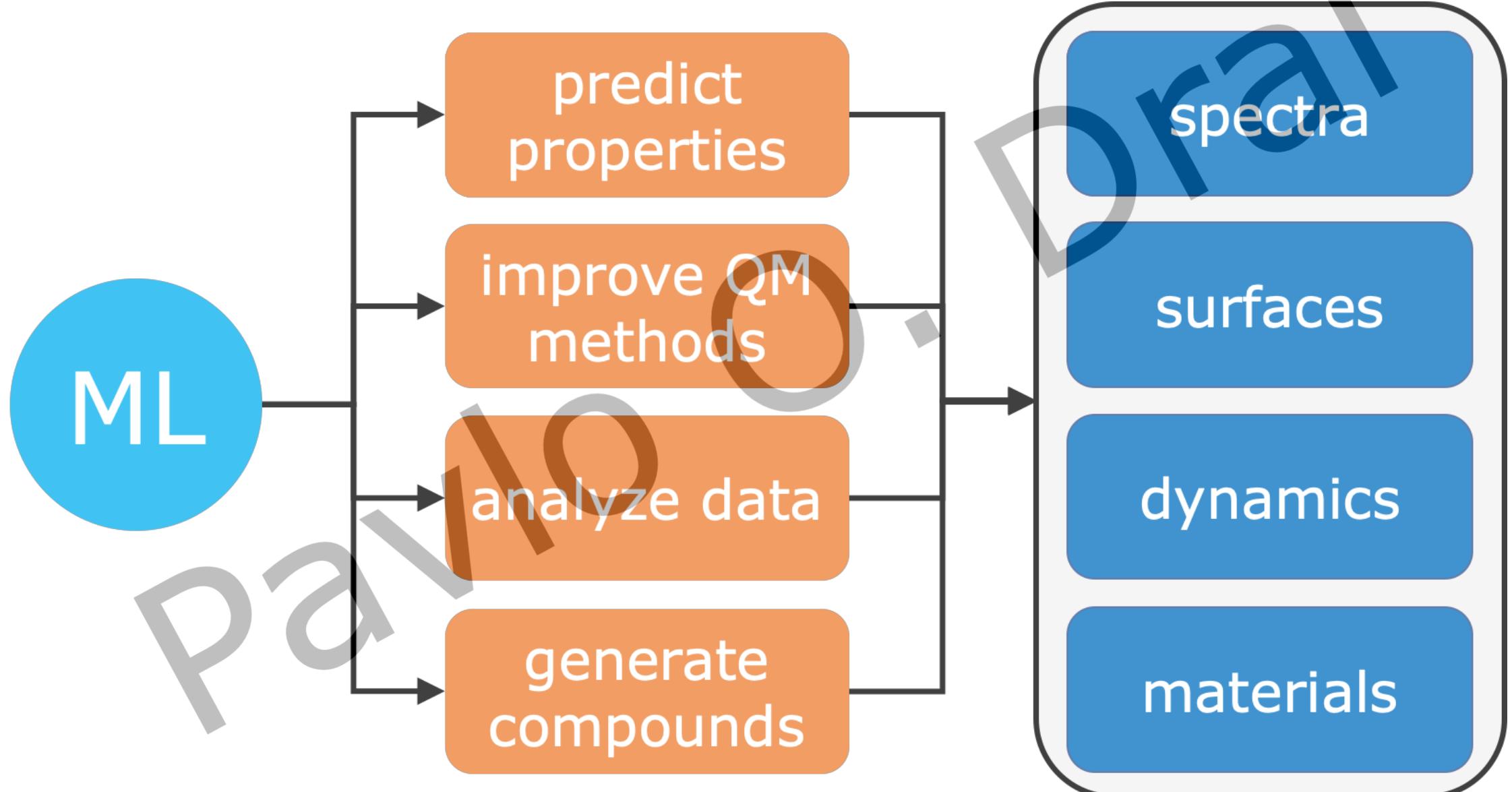
**Air Photo: CC BY-SA 3.0,**  
<https://commons.wikimedia.org/w/index.php?curid=27584741>



Xiamen University, Siming campus

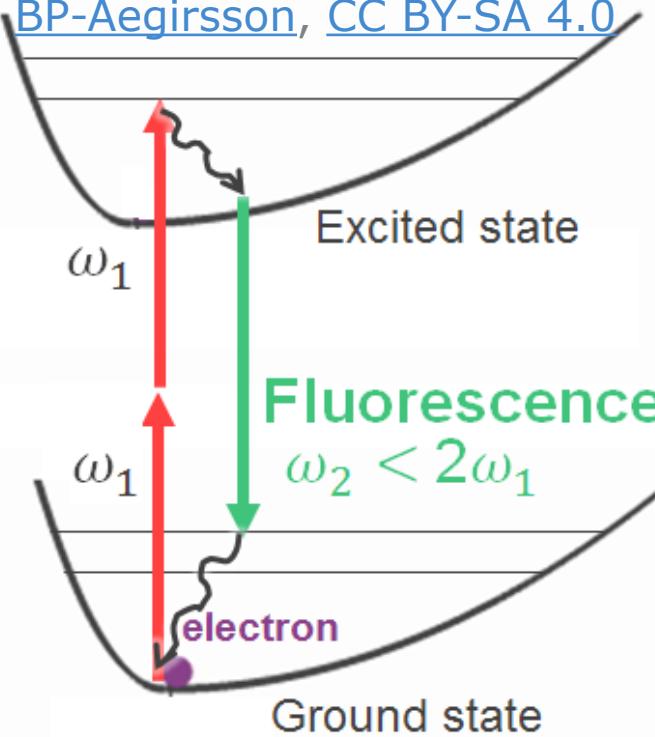
16 subjects rank top 1% globally. 11th in Mainland China.

Chemistry ranks top 1% globally (ESI as of March 2019).



# Two-photon absorption

[BP-Aegirsson, CC BY-SA 4.0](#)

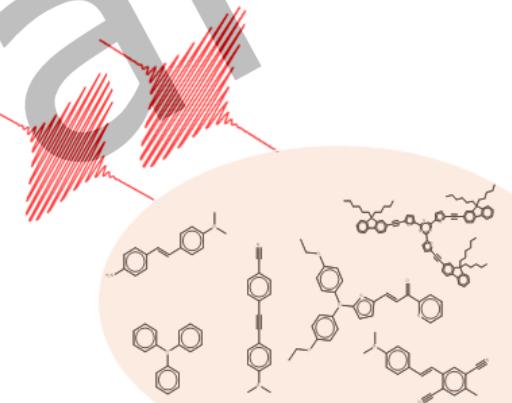
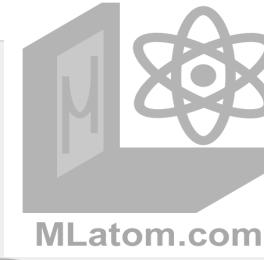


## Two-photon absorption applications:

- two-photon lithography
- Photodynamic therapy
- Bioimaging
- 3D printing
- Upconverted laser

Here we show how to calculate TPA cross section for RHODAMINE 6G and RHODAMINE 123 molecules with MLatom input file `mltpa.inp`:

MLTPA  
`SMILESfile=Smiles.csv`  
`auxfile=_aux.txt`



This input requires `Smiles.csv` file with SMILES of molecules:

```
CCNC1=CC2=C(C=C1C)C(=C3C=C(C([NH+]CC)C=C3O2)C)C4=CC=CC=C4C(=O)OCC.[Cl-]
COC(=O)C1=CC=CC=C1C2=C3C=CC(=N)C=C3O4=C2C=CC(=C4)N.Cl
```



Yuming Su

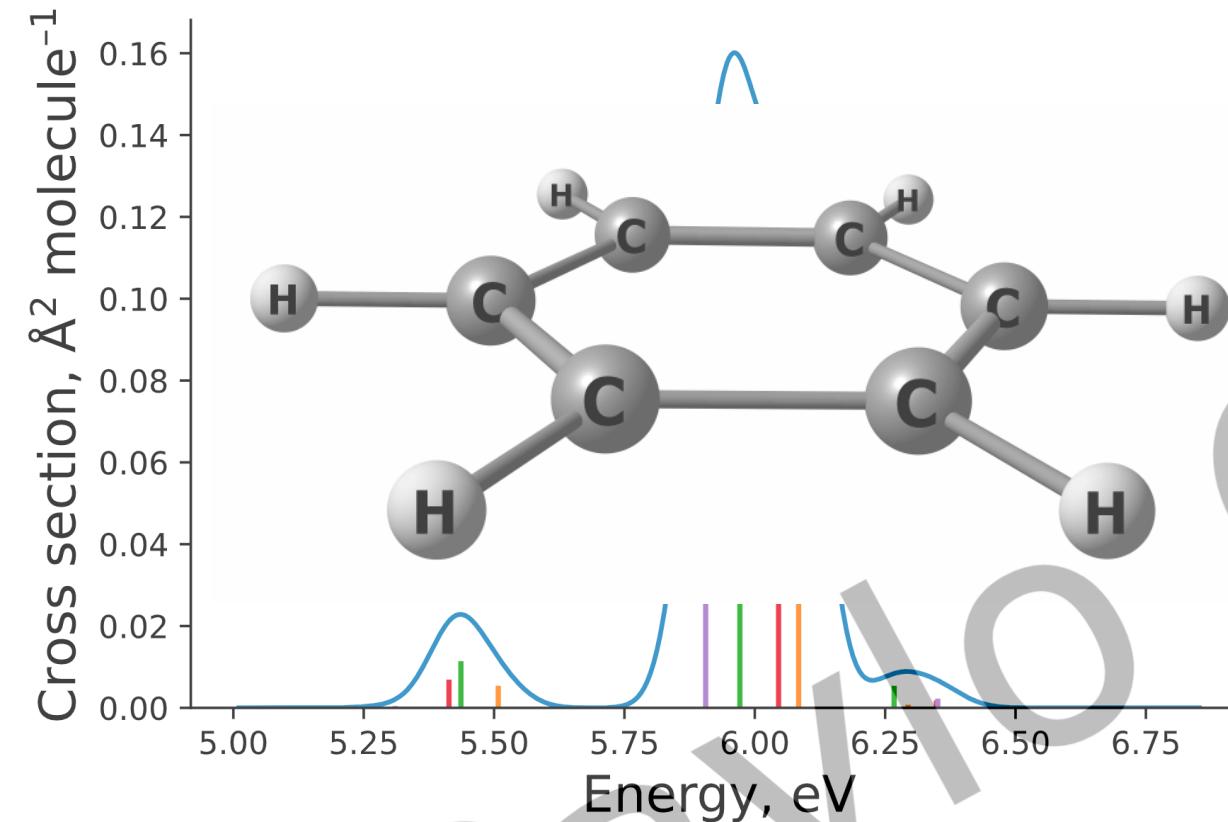


Zhou Da



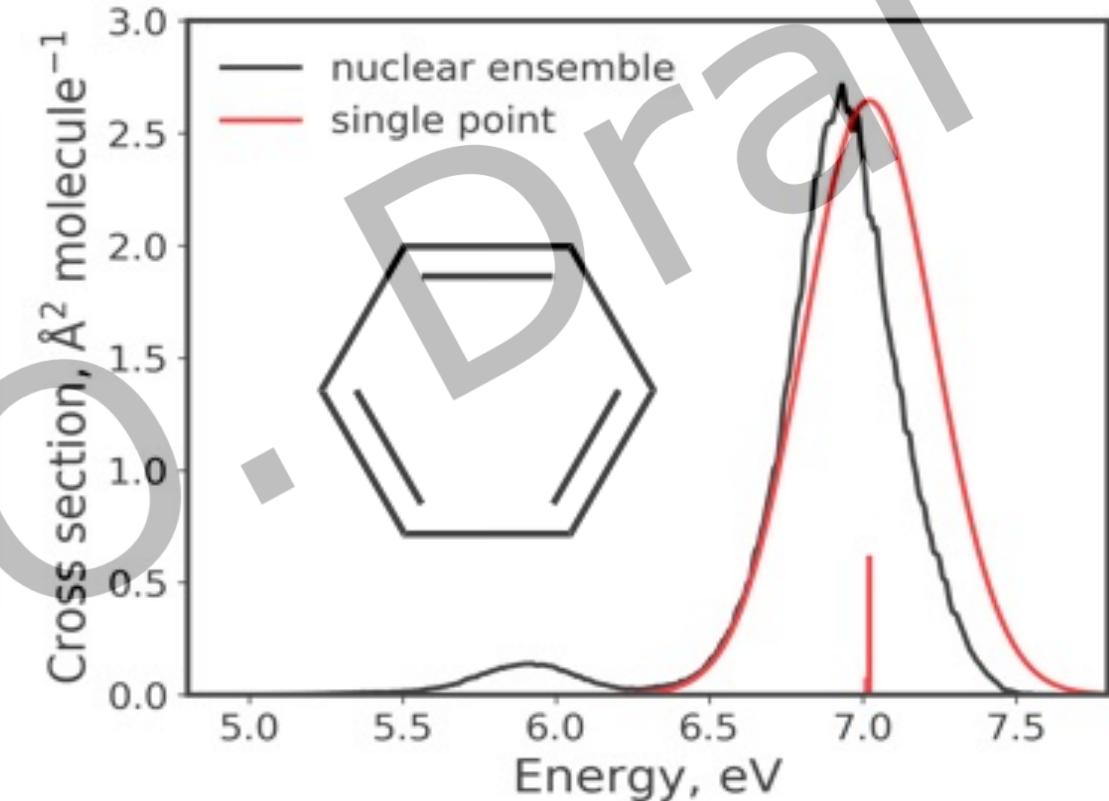
Cheng Wang

# Machine learning UV-vis absorption spectra



Nuclear Ensemble Approach (NEA) calculates cross section by averaging over multiple normalized broadening functions at different conformations (marked by different colors).

$$\sigma(E) = \frac{\pi e^2 h}{2mc\epsilon_0 E} \sum_n^{N_{fs}} \frac{1}{N_p} \sum_i^{N_p} \Delta E_{0n}(\mathbf{x}_i) f_{0n}(\mathbf{x}_i) \frac{1}{\sqrt{2\pi(\delta/2)^2}} \exp\left(-\frac{(E - \Delta E_{0n})^2}{2(\delta/2)^2}\right)$$



Compared with the single point convolution, NEA correctly predicts absorption intensity for forbidden transitions (example: benzene)

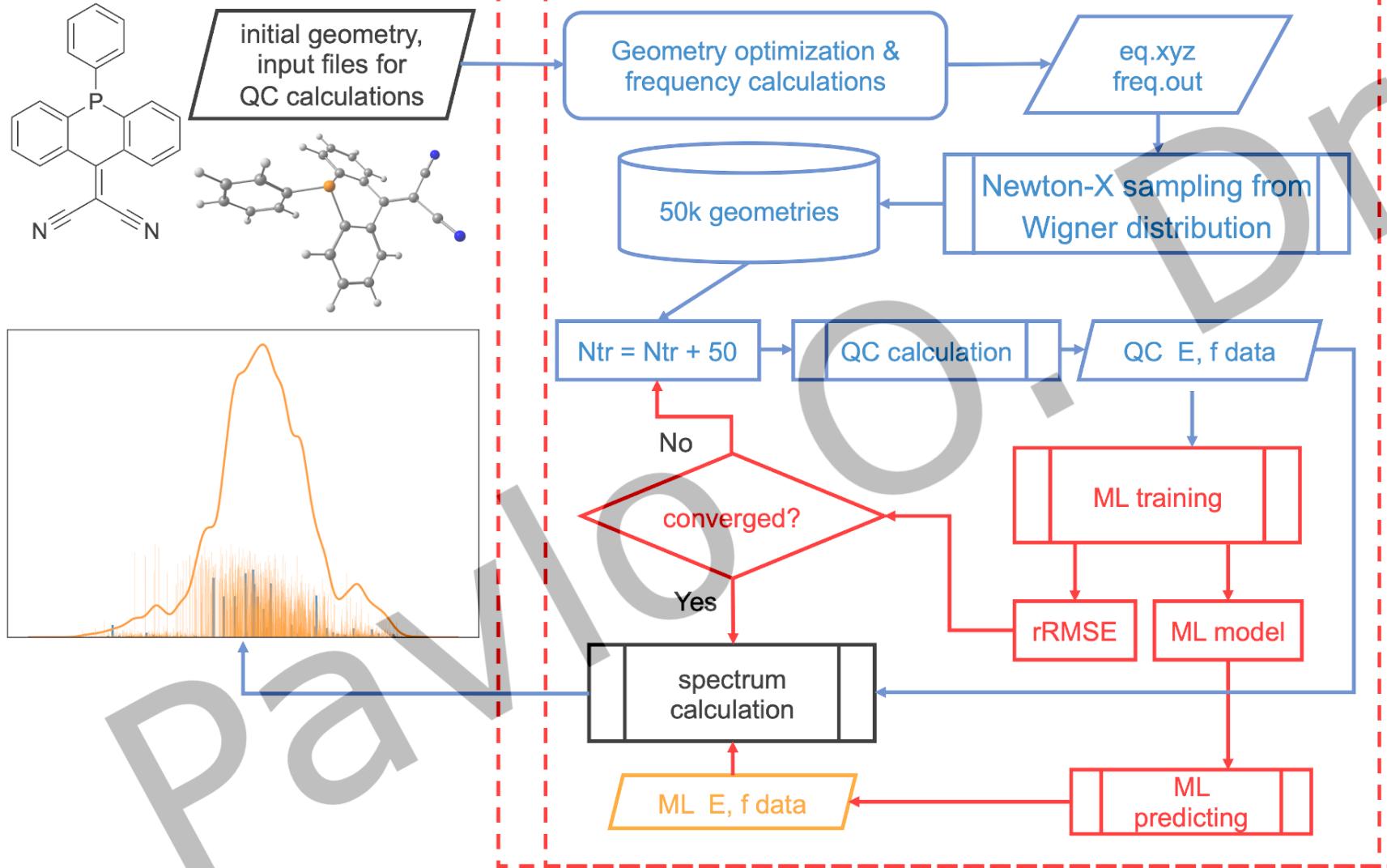
Conventional programming in quantum chemistry:

- Code for molecular orbitals
- Code for excitation energies
- Code for oscillator strengths
- ...

Machine learning (in principle – adaptations required!):

- The same code for all above
- ↑  
MOs                    excitation energies                    Oscillator strength  
Training data

# Machine learning single-photon absorption spectra



Mario  
Barbatti



Bao-Xin  
Xue

ML-NEA method: B.-X. Xue, P. O. Dral, M. Barbatti, *J. Phys. Chem. A* **2020**, 124, 7199–7210

Implementation in MLatom: P. O. Dral, F. Ge, B.-X. Xue, Y.-F. Hou, M. Pinheiro Jr, J. Huang, M. Barbatti, *Top. Curr. Chem.*, **2021**, 379, 27

## Simulations

- single-point calculations
- geometry optimizations (minima and transition states, IRC)
- frequencies & thermochemistry
- UV/vis spectra (ML-NEA)
- simulations with pre-trained models (AIQM1, ANI-1ccx, etc.)
- simulations with user-trained models
- **NEW!** two-photon absorption cross sections (ML-TPA)
- Only available on MLatom@XACS cloud:
  - quantum dynamics with machine learning
- Coming soon:
  - molecular dynamics
  - IR spectra

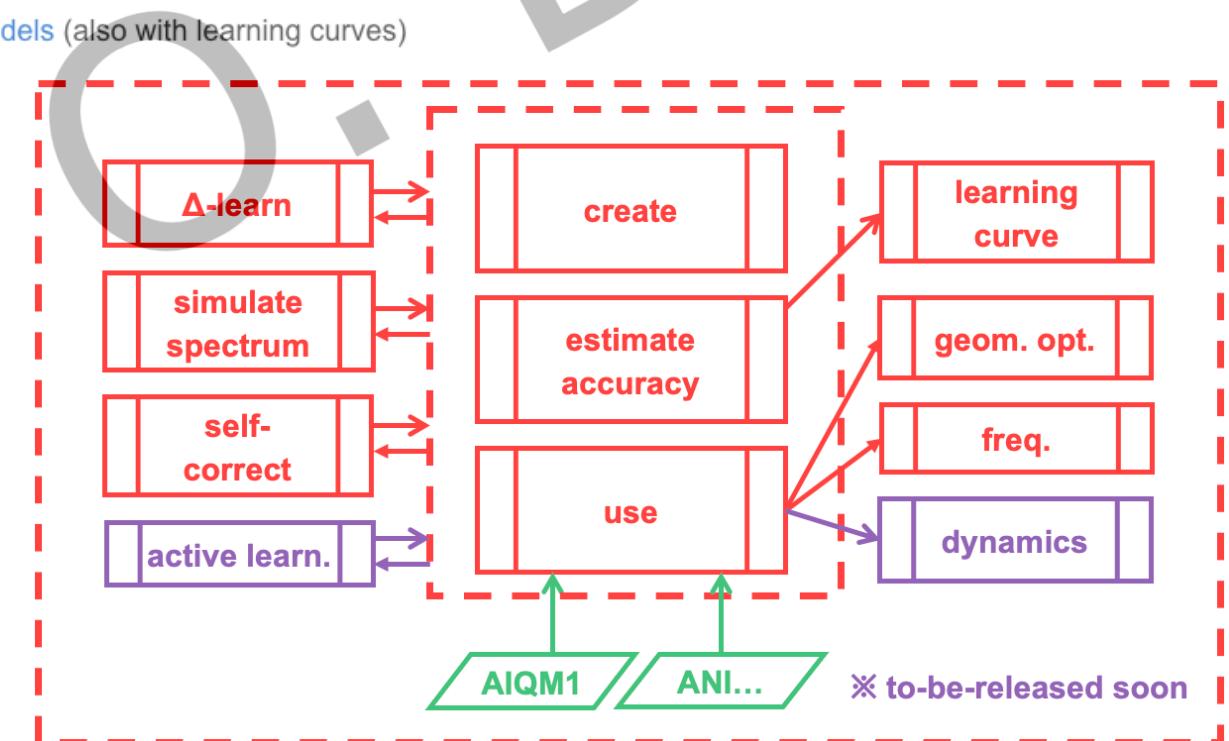


## Learning

- training popular ML models (KREG, ANI, sGDML, PhysNet, DPMD, GAP-SOAP, KRR-CM)
- training generic ML models (kernel ridge regression with many kernels)
- optimizing hyperparameters
- evaluating ML models (also with learning curves)
- $\Delta$ -learning
- self-correction

## Data

- converting XYZ coordinates to molecular descriptor (RE, Coulomb matrix, ...)
- analyzing data sets
- sampling (random, structure-based, farthest-point) and splitting datasets





**XACS**  
Xiamen Atomistic  
Computing Suite

**XMVB**

**XEDA**

**MLatom**

**Cloud computing (free!)**



[XACScloud.com](http://XACScloud.com)

- *Ab initio* valence bond calculations (**VBSCF**, **VBCI**, **BOVB**, ...)
- Generalized Kohn–Sham energy decomposition analysis (**GKS-EDA**)
- Artificial intelligence-enhanced quantum mechanical method 1 (**AIQM1**, faster and more accurate than B3LYP)
- Fast geometry optimization, MD, thermochemistry
- ... and much more

**Principal investigators (Xiamen University)**

- Wei Wu
- Peifeng Su
- Pavlo O. Dral

**Partners**

- Mario Barbatti, Aix Marseille University
- Benoît Braïda, Sorbonne Université
- Philippe Hiberty, University of Paris-Saclay
- Olexandr Isayev, Carnegie Mellon University
- Yirong Mo, UNC Greensboro
- Sason Shaik, Hebrew University
- Avital Shurki, Hebrew University
- Cheng Wang, Xiamen University

**Interfaces**

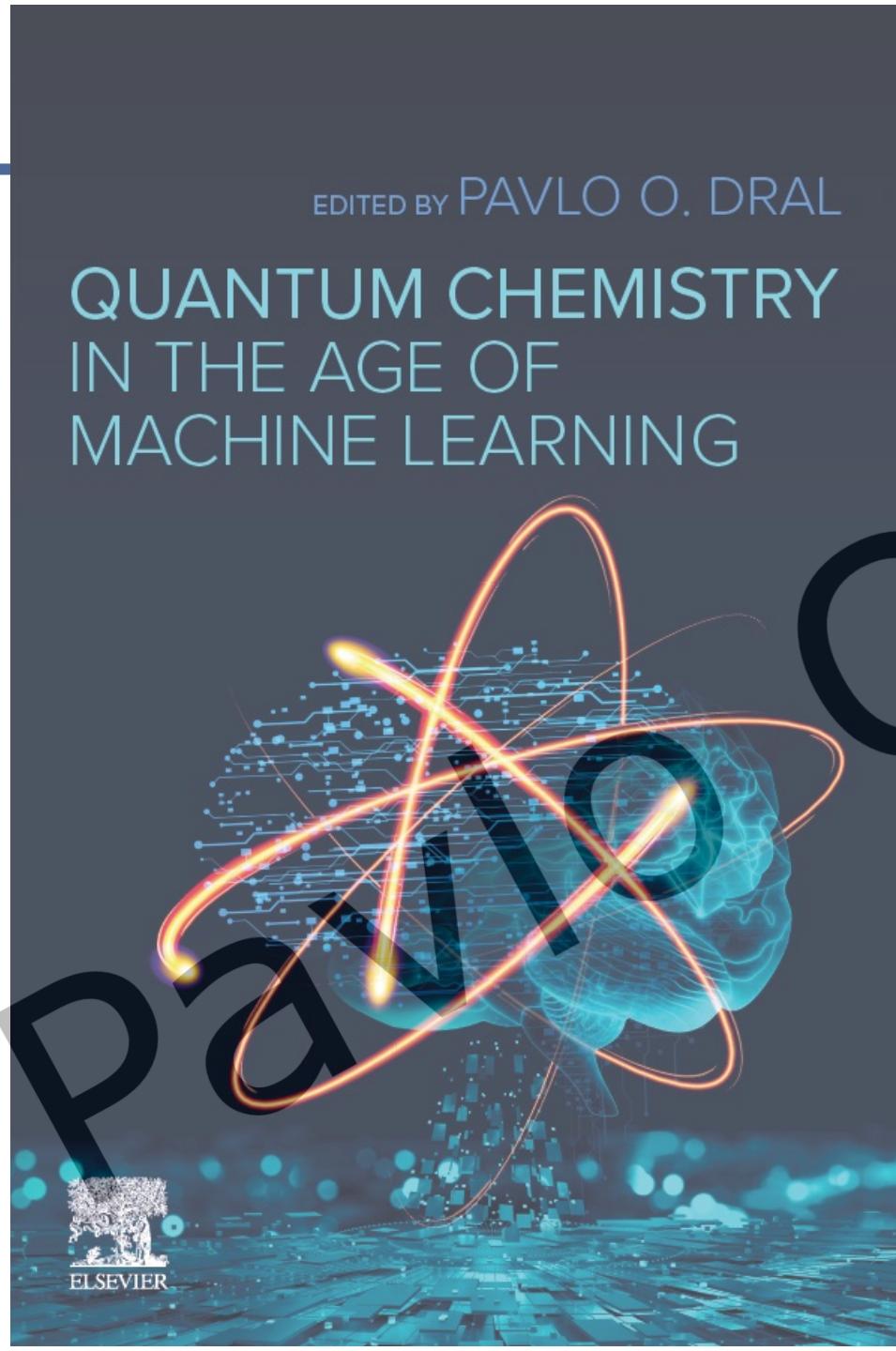
TorchANI

SPARROW

ASE hyperopt



Published in  
September  
2022



EDITED BY PAVLO O. DRAL

# QUANTUM CHEMISTRY IN THE AGE OF MACHINE LEARNING

Chapter	Title
	Preface
<b>Part 1</b>	<b>Introduction</b>
1	Very brief introduction to quantum chemistry
2	Density functional theory
3	Semiempirical quantum mechanical methods
4	From small molecules to solid-state materials: A brief discourse on an example of carbon compounds
5	Basics of dynamics
6	Machine learning: An overview
7	Unsupervised learning
8	Neural networks
9	Kernel methods
10	Bayesian inference
<b>Part 2</b>	<b>Machine learning potentials</b>
11	Potentials based on linear models
12	Neural network potentials
13	Kernel method potentials
14	Constructing machine learning potentials with active learning
15	Excited-state dynamics with machine learning
16	Machine learning for vibrational spectroscopy
17	Molecular structure optimizations with Gaussian process regression
<b>Part 3</b>	<b>Machine learning of quantum chemical properties</b>
18	Learning electron densities
19	Learning dipole moments and polarizabilities
20	Learning excited-state properties
<b>Part 4</b>	<b>Machine learning-improved quantum chemical methods</b>
21	Learning from multiple quantum chemical methods: $\Delta$ -learning, transfer learning, co-kriging, and beyond
22	Data-driven acceleration of coupled-cluster and perturbation theory methods
23	Redesigning density functional theory with machine learning
24	Improving semiempirical quantum mechanical methods with machine learning
25	Machine learning wavefunction
<b>Part 5</b>	<b>Analysis of Big Data</b>
26	Analysis of nonadiabatic molecular dynamics trajectories
27	Design of organic materials with tailored optical properties: Predicting quantum-chemical polarizabilities and derived quantities

27 chapters  
65 authors!

## Case study

This case study uses the KREG model to fit the PES of the hydrogen molecule and then uses this KMP to get the optimized bond length of H<sub>2</sub>. All the data, input files, and instructions are also described at <https://github.com/dralgroup/MLinQCbook22-KMP>. The calculations will be done with the MLatom package [11,22,23] for atomistic machine learning simulations using the data set with 451 Cartesian (XYZ) geometries of H<sub>2</sub> and full configuration interaction (FCI) energies calculated with the aug-cc-pV6Z basis set. This data set is taken from Ref. [32].

The case study consists of two simple steps.

### Step 1. Training the KREG potential

To train the KREG potential, we need both geometries and reference energies, which come with the data set. In addition, we need to choose the initial guess for the equilibrium geometry to obtain  $r_{a,b \neq a}^{\text{eq}}$  terms in the RE descriptor as defined by Eq. (6). Here we choose a geometry with H—H bond length of 0.8 Å as an initial guess of the equilibrium structure saved in the eq.xyz file:

```
2
H 0.000000 0.000000 0.000000
H 0.000000 0.000000 0.800000
```

After that we can train the KREG model on the entire data set with MLatom using the following input file (the comments are given after "#" symbol):

Book chapter 13:

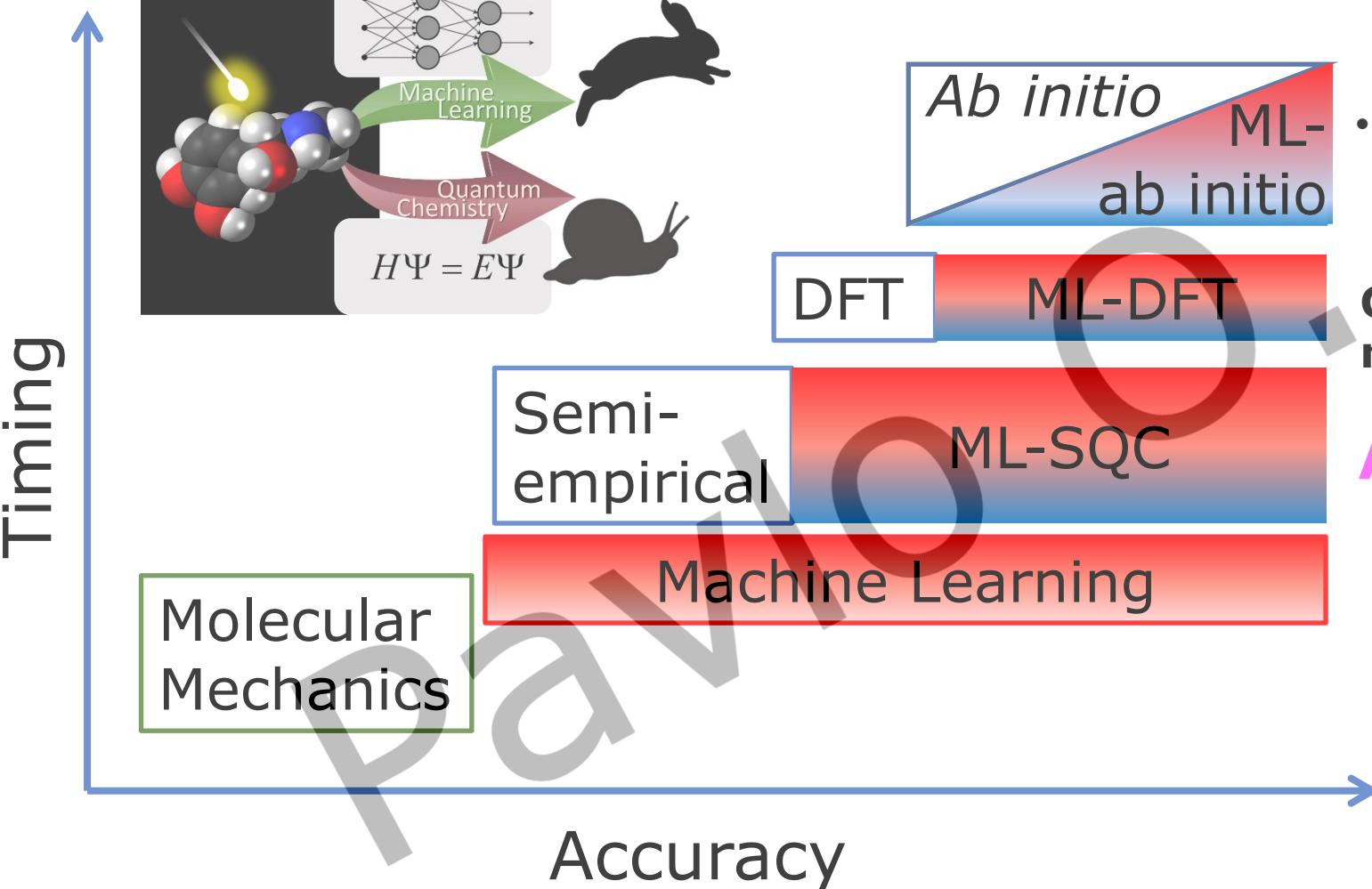
Yi-Fan Hou and Pavlo O.  
Dral. Kernel method  
potentials.

In Quantum Chemistry in  
the Age of Machine  
Learning,  
Pavlo O. Dral, Ed. Elsevier:  
2023.

DOI: 10.1016/B978-0-323-  
90049-2.00020-2.

# Machine learning in quantum chemistry

P. O. Dral, M. Barbatti, *Nat. Rev. Chem.* **2021**, *5*, 388



## Concepts:

- Delta-learning  
R. Ramakrishnan, P. O. Dral, M. Rupp, O. A. von Lilienfeld. *JCTC* **2015**
- Learning Hamiltonian  
P. O. Dral, O. A. von Lilienfeld, W. Thiel. *JCTC* **2015**, *11*, 2120

## General-purpose (no training required):

**AIQM1** AIQM1: P. Zheng, R. Zubatyuk, W. Wu, O. Isayev, P. O. Dral, *Nat. Commun.* **2021**, *12*, 7022

# Accuracy vs transferability vs cost



Wei Wu      Olexandr Isayev

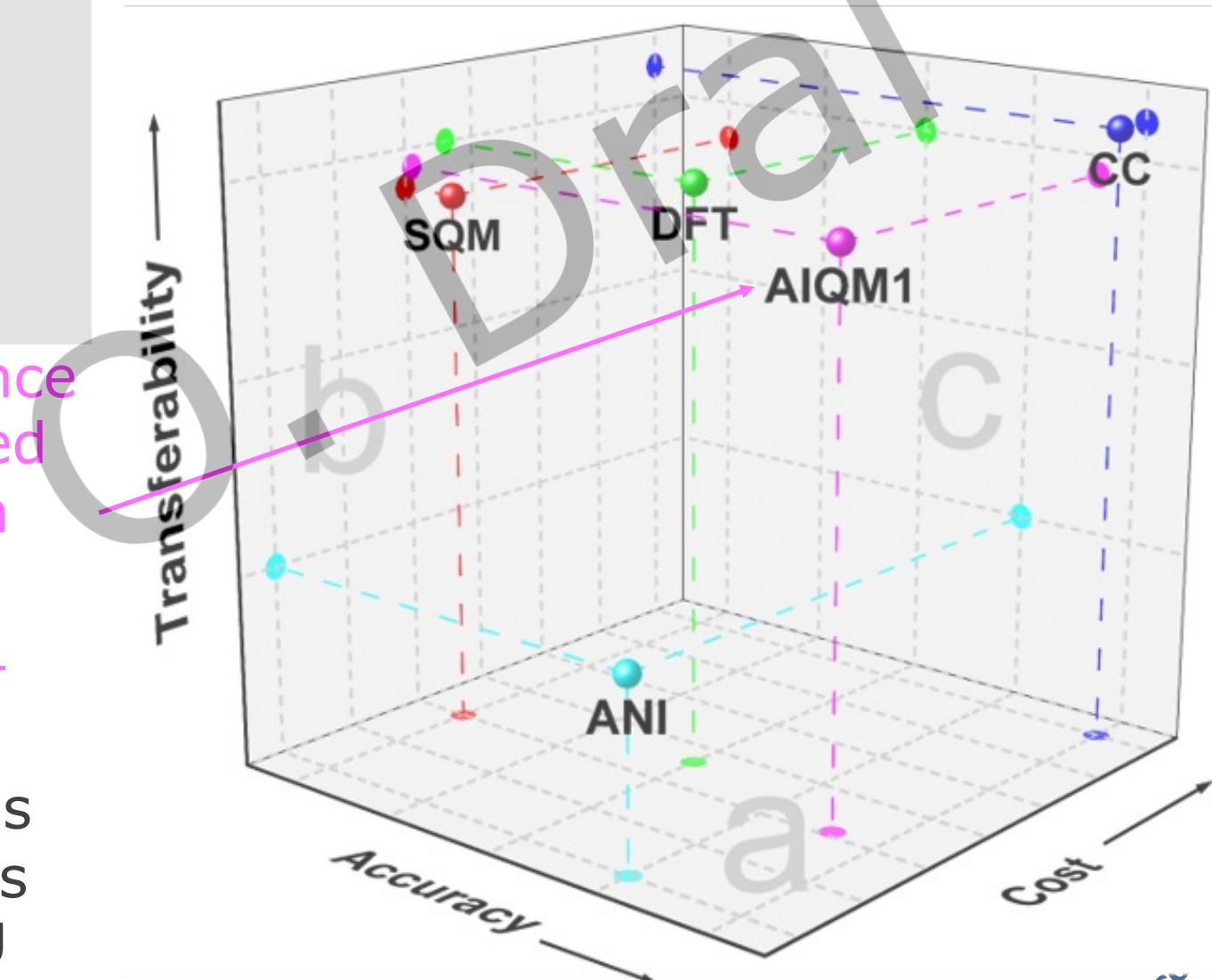


Peikun Zheng      Roman Zubatyuk

CCSD(T)\*/CBS SP: 69 h /15 CPUs  
 DFT opt: 30 min /32 CPUs  
 AIQM1 opt: 14 sec / 1 CPU

$$\text{AIQM1} = \text{SQM} + \Delta \text{SQM} + \text{D4}$$

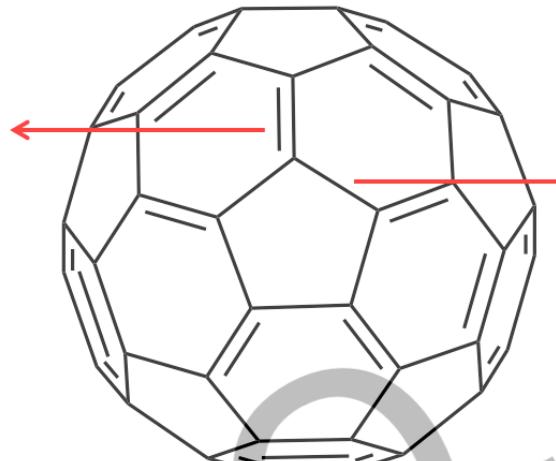
Intelligence-Enhanced Quantum Chemical Method 1  
**AIQM1**



# Ground-state geometries

**a**

1.355–1.401 (experiment)  
**1.393 (AIQM1)**  
**1.388 (AIQM1@DFT(\*)**)  
 1.379 ( $\omega$ B97X(-D4)/  
 def2-TZVPP)  
**1.451 (ANI-1ccx)**



1.432–1.467 (experiment)  
**1.467 (AIQM1)**  
**1.464 (AIQM1@DFT(\*)**)  
 1.448 ( $\omega$ B97X(-D4)/  
 def2-TZVPP)  
**1.451 (ANI-1ccx)**

**c** MGHBL9 and MGNHBL11 benchmark

$\text{H}_3\text{C}-\text{H}$   
 1.086  
**1.086**

$\text{H}-\text{H}$   
 0.741  
**0.726**

$\text{HO}-\text{H}$   
 0.957  
**0.958**

$\text{HC}\equiv\text{C}-\text{H}$   
 1.203 1.063  
**1.205** 1.064

$\text{N}\equiv\text{C}-\text{H}$   
 1.153 1.065  
**1.152** 1.065

$\cdot\text{O}-\text{H}$   
 0.970  
**0.959**

$-\text{N}=\text{N}^+=\text{O}$  experiment  
 1.128 1.184  
**1.120** 1.186

$\text{OC}=\text{O}$   
 1.160  
**1.160**

$\text{O}=\text{C}(\text{H})-\text{H}$   
 1.203 1.101  
**1.205** 1.101

$\text{H}_2\text{N}-\text{H}$   
 1.012  
**1.012**

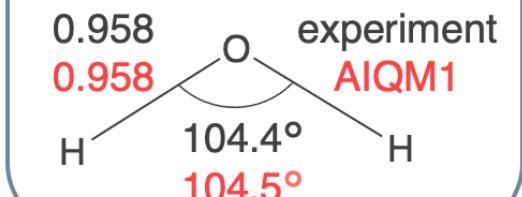
theoretical reference  
 AIQM1

$\text{N}\equiv\text{N}$   
 1.098  
**1.097**

$-\text{C}\equiv\text{O}^+$   
 1.128  
**1.125**

**b**  $\text{H}_2\text{O}$  in CHNO benchmark

0.958  
**0.958**



A diagram of a water molecule (H<sub>2</sub>O) in its ground state. The oxygen atom is at the top, with two hydrogen atoms at the bottom-left and bottom-right. The angle between the two hydrogen atoms is labeled as 104.4°. The text "experiment" is written next to the oxygen atom, and "AIQM1" is written next to one of the hydrogen atoms.

data set	ODM2	B3LYP/ 6-31G*	$\omega$ B97X/ 6-31G*	$\omega$ B97X-D/ 6-31G*	$\omega$ B97X/ def2-TZVPP	$\omega$ B97X-D4/ def2-TZVPP	ANI- 1ccx	AIQM1 @DFT*	AIQM1 @DFT	AIQM1	CCSD(T)* /CBS
energies, kcal/mol											
CHNO	2.64	6.71	4.10	3.84	3.21	2.76	—	2.49	2.12	0.87	—
G3/99	3.04	8.53	3.46	3.22	4.18	3.20	—	2.83	2.06	0.88	—
ISOMERS44 ( $\Delta H_f$ )	1.16	8.08	3.57	3.53	4.52	3.78	—	3.00	2.27	0.42	—
ISOMERS44 ( $\Delta H_r$ )	0.70	2.29	1.45	1.31	1.19	1.10	1.68	0.95	0.89	0.50	—
IsoL6/11	1.48	5.26	3.83	3.36	1.75	1.64	1.46	1.65	1.55	0.62	0.47
HC7/11	5.37	6.44	16.90	13.98	6.83	7.10	2.53	8.89	9.16	1.43	1.57

Heats of formation

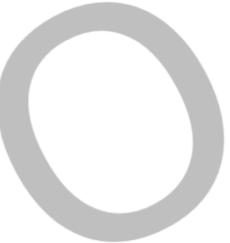
## Ground-state properties of neutral, closed-shell compounds (heats of formation, reaction enthalpies, and ZPVE-exclusive reaction energies)

Torsion	0.74	0.55	0.30	0.29	0.20	0.19	0.23	0.23	0.23	0.19	0.05
bond lengths, Å											
CHNO	0.015	0.006	0.008	0.007	0.010	0.010	0.011	0.010	0.010	0.007	—
MGHBL9	0.023	0.007	0.006	0.005	0.002	0.002	0.047	0.011	0.011	0.004	—
MGNHBL11	0.026	0.006	0.003	0.002	0.008	0.008	0.004	0.008	0.008	0.002	—
bond angles, °											
CHNO	2.04	0.70	0.68	0.64	0.68	0.68	1.00	0.77	0.77	0.70	—
dihedral angles, °											
CHNO	4.07	5.20	4.68	6.10	7.12	7.11	5.86	2.14	2.14	2.31	—

# Revising experimental heats of formation



CHNO data set

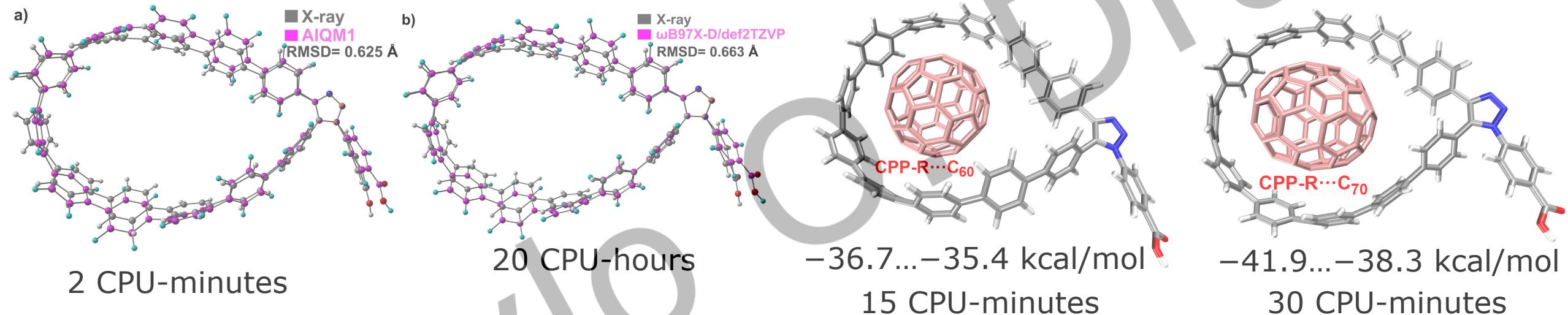


1,3-pyrimidine  
exper.: 46.8  
AIQM1: 44.5  
G4: 44.3



acrolein  
exper.: -18  
AIQM1: -16.0  
G4: -15.9

❖ Quality of theoretically optimized geometries ❖ Interaction with fullerenes at AIQM1



AIQM1/CIS also correctly predicted that the fluorescence of cycloparaphenylenes is quenched after complexation with fullerenes

T. A. Schaub, A. Zieleniewska, R. Kaur, M. Minameyer, W. Yang, C. M. Schüßlbauer, L. Zhang, M. Freiberger, L. N. Zakharov, T. Drewello, P. O. Dral, D. Guldi, R. Jasti. Tunable Macrocyclic Polyparaphylene Nanolassos via Copper-Free Click Chemistry. *Chem. Eur. J.* **2023**.

# Unpublished: Infrared spectra with AIQM1

Long MD trajectory is needed!

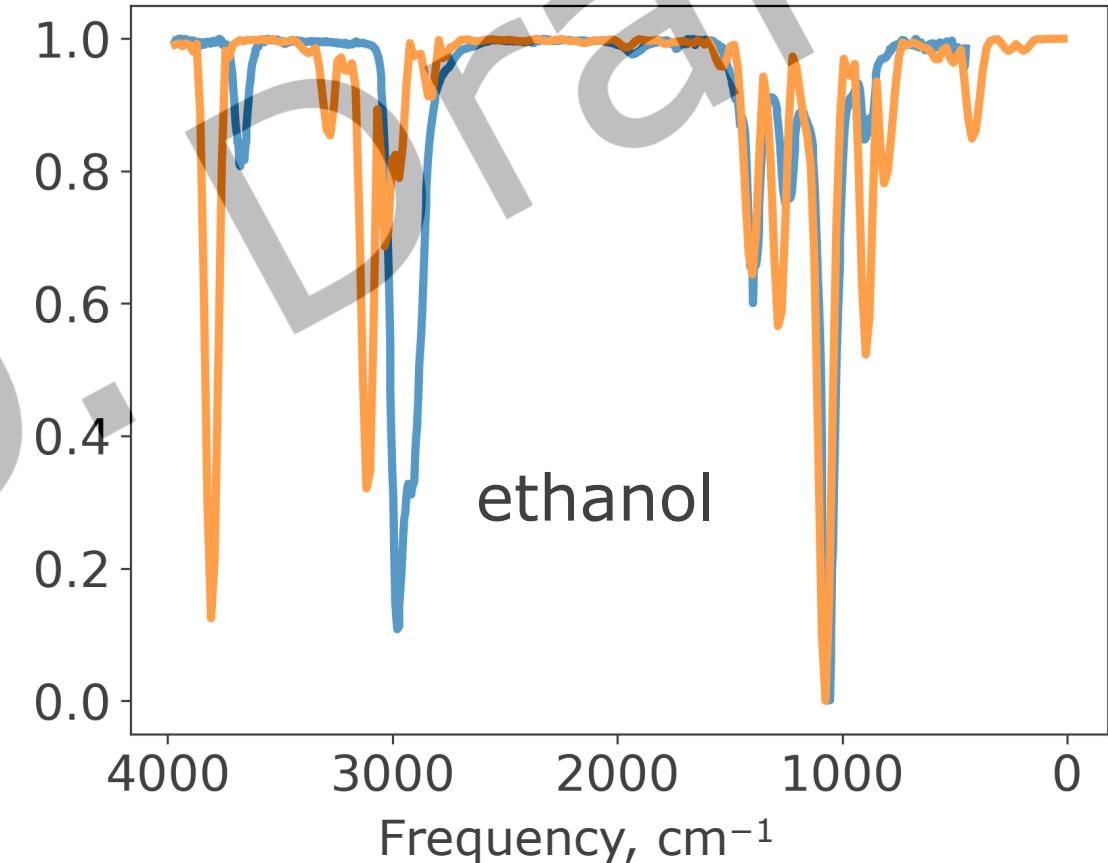
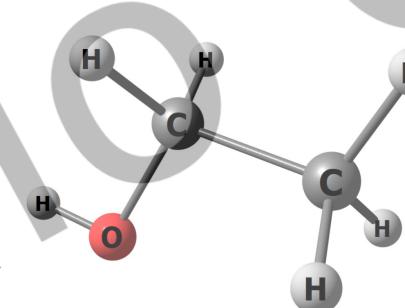
IR intensities:[1,2]

$$P(\omega) \propto \int \langle \dot{\mu}(\tau) \dot{\mu}(t + \tau) \rangle_{\tau} e^{-i\omega t} dt$$

$$P(\omega) \propto \omega \tanh\left(\frac{\hbar\omega}{2k_B T}\right) \int \langle \mu(\tau) \mu(t + \tau) \rangle_{\tau} e^{-i\omega t} dt$$



Implementation by  
Yi-Fan Hou



Experiment (NIST)  
AIQM1 MD (by Yifan Hou, unpublished)  
200 ps trajectory at 300 K

[1] Phys. Chem. Chem. Phys. **2013**, 15, 6608

[2] Phys. Chem. Chem. Phys. **2016**, 28325

To propagate molecular dynamics:

- We just need forces → can be obtained efficiently from machine learning potentials

$$F_{A,d} = M_A a_{A,d}$$

$$a_{A,d} = F_{A,d} \frac{1}{M_A}$$

$$\frac{\partial^2 x_{A,d}}{\partial t^2} = F_{A,d} \frac{1}{M_A}$$

$$F = -\frac{\partial E}{\partial x_{A,d}} = -\frac{\partial E \text{ machine learning potential}(\mathbf{x})}{\partial x_{A,d}}$$

$$F = -\frac{\partial E}{\partial r}$$

$$\frac{\partial^2 \mathbf{r}_{A,d}}{\partial t^2} = -\frac{\partial E}{\partial \mathbf{r}_{A,d}} \frac{1}{M_A}$$

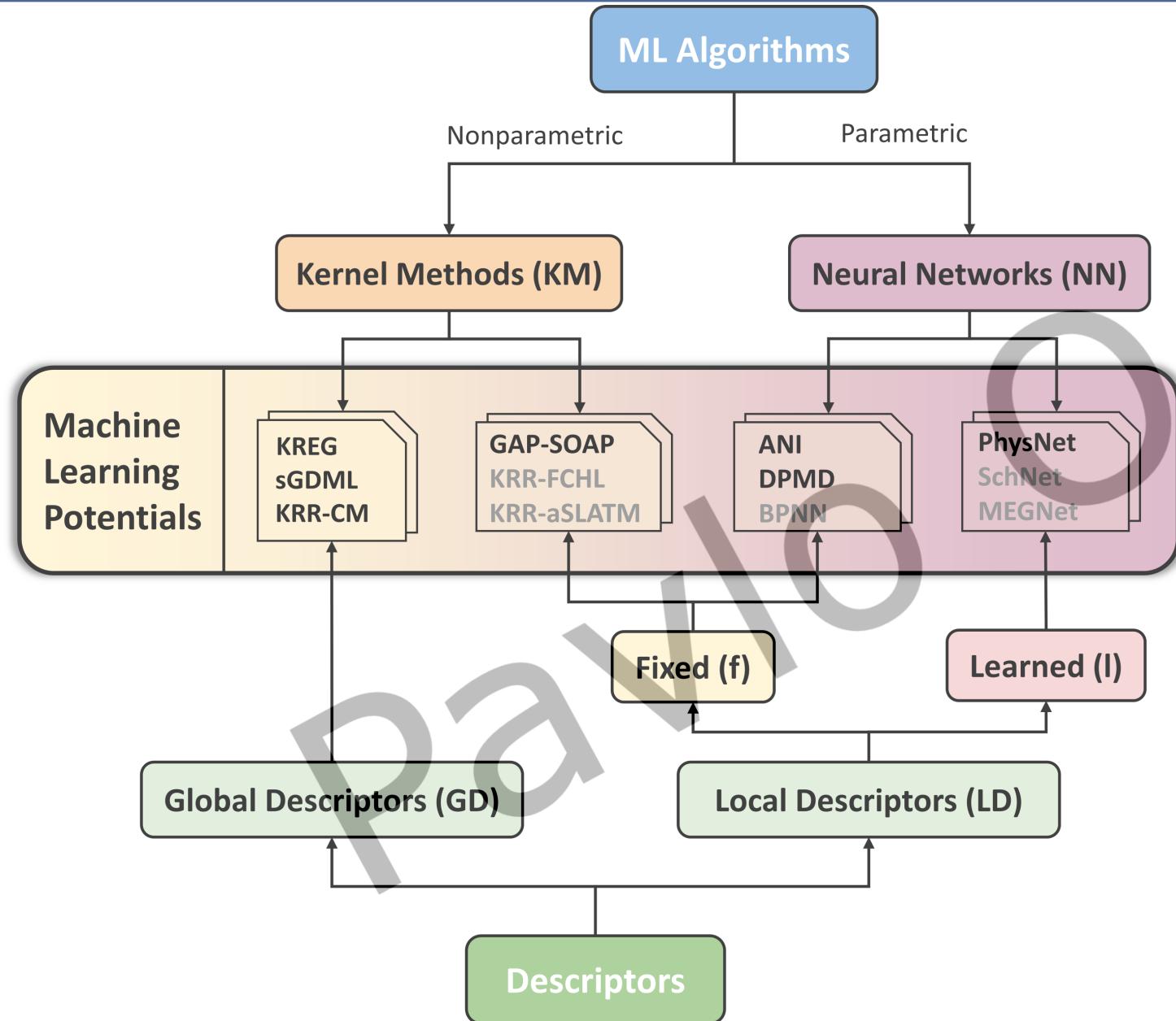
Velocity Verlet algorithm:

$$\mathbf{x}(t + \Delta t) = \mathbf{x}(t) + \mathbf{v}(t)\Delta t + \frac{1}{2}\mathbf{a}(t)\Delta t^2$$

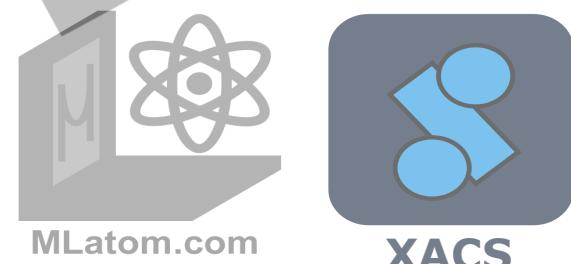
$$\mathbf{v}(t + \Delta t) = \mathbf{v}(t) + \frac{1}{2}[\mathbf{a}(t) + \mathbf{a}(t + \Delta t)]\Delta t,$$

where  $\mathbf{x}$  is the coordinate,  $\mathbf{v}$  – the velocity,  $\mathbf{a}$  – the acceleration,  $t$  – the time and

# Categories of machine learning potentials



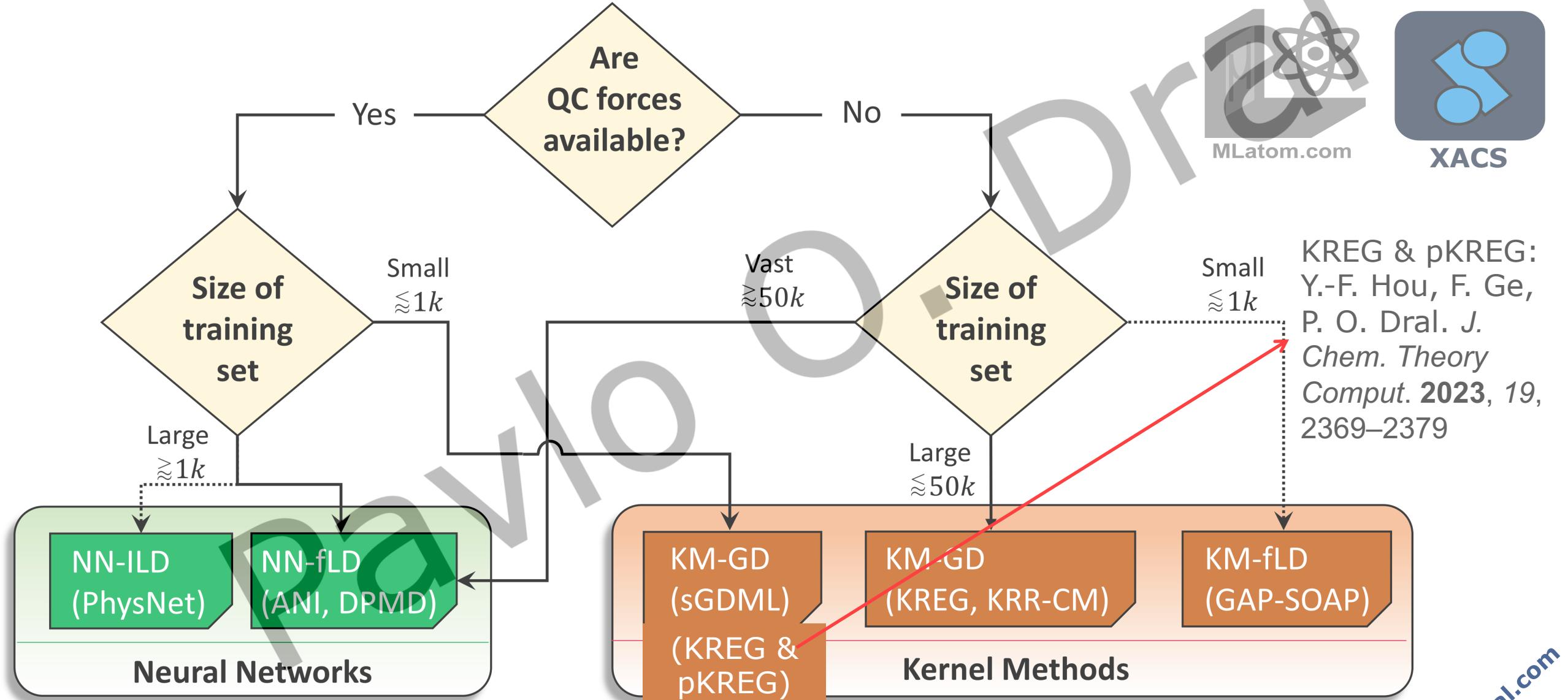
Models implemented/interfaced in MLatom  
not implemented in MLatom



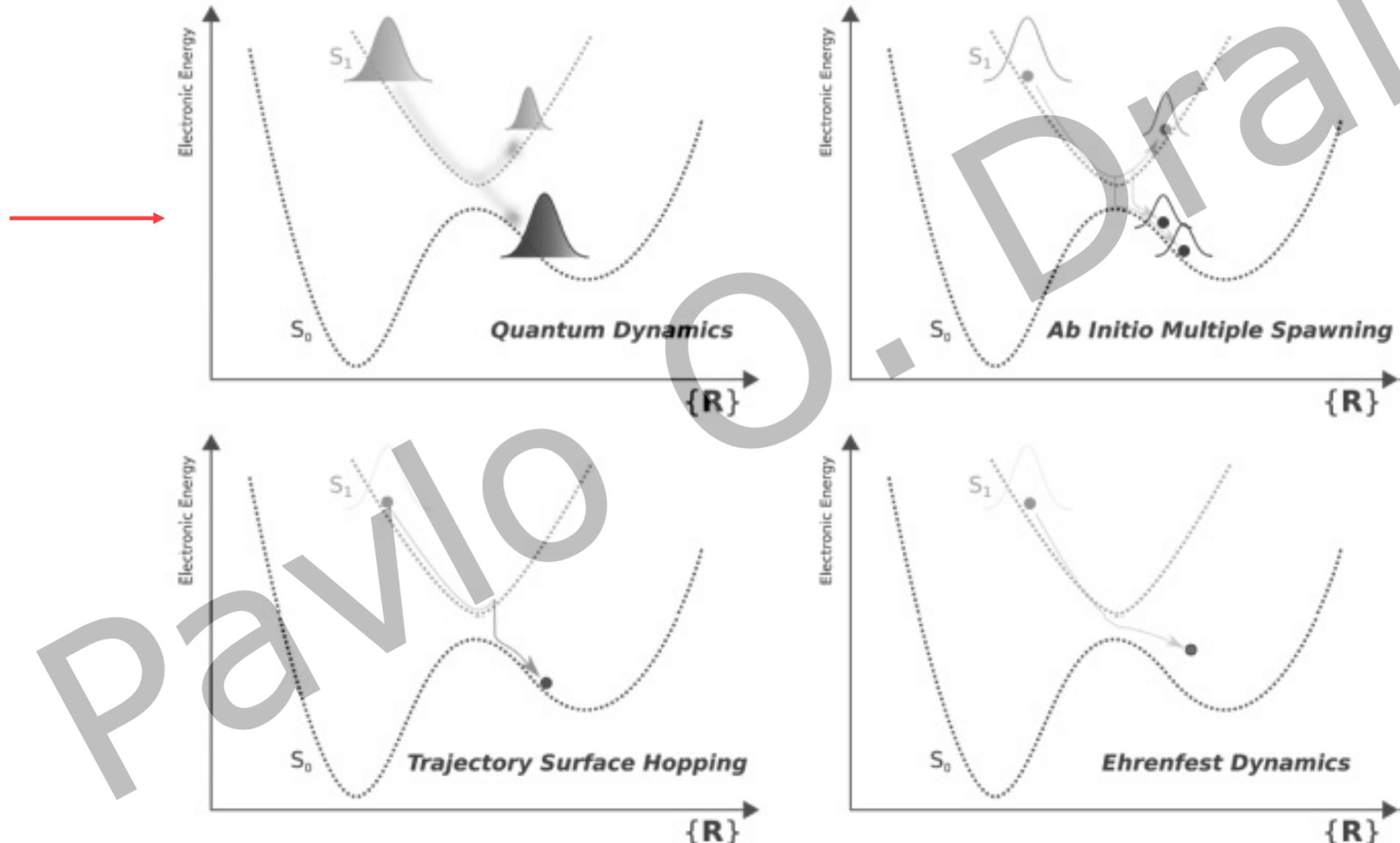
M. Pinheiro Jr, F. Ge, N. Ferré, P. O. Dral, M. Barbatti. *Chem. Sci.* **2021**, 12, 14396–14413

P. O. Dral, F. Ge, B.-X. Xue, Y.-F. Hou, M. Pinheiro Jr, J. Huang, M. Barbatti. *Top. Curr. Chem.* **2021**, 379, 27

# Choosing the 'Right' ML Potential



# Many flavors for quantum dynamics (QD)



# Machine learning to speed up dynamics

$$\rho(t) = f[\rho(t - \Delta t)]$$

dynamics propagation is

- computationally expensive

dynamics

ML dynamics

$$\rho(t) = f^{\text{ML}}[\rho(t - \Delta t)]$$

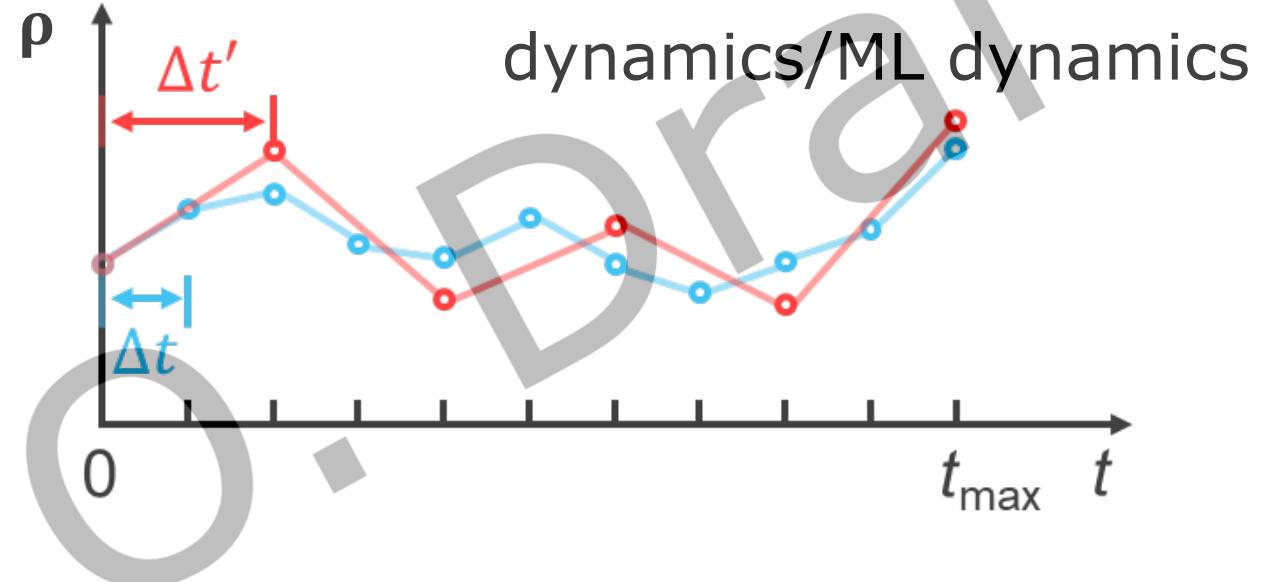
PAVLO · DRAL

# Can we do better?

$$\rho(t) = f[\rho(t - \Delta t)]$$

dynamics propagation is

- computationally expensive
- recursive (iterative)



PAVIO

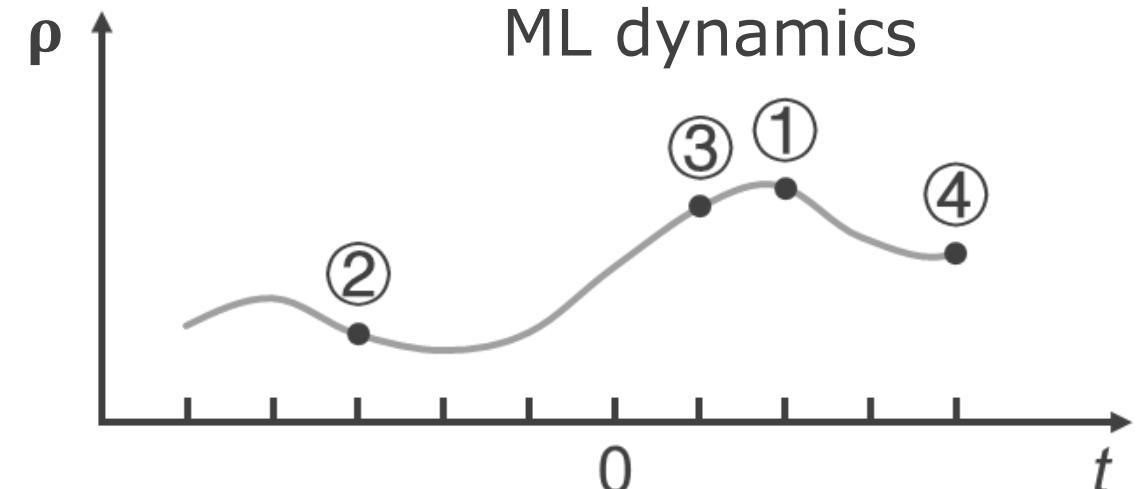
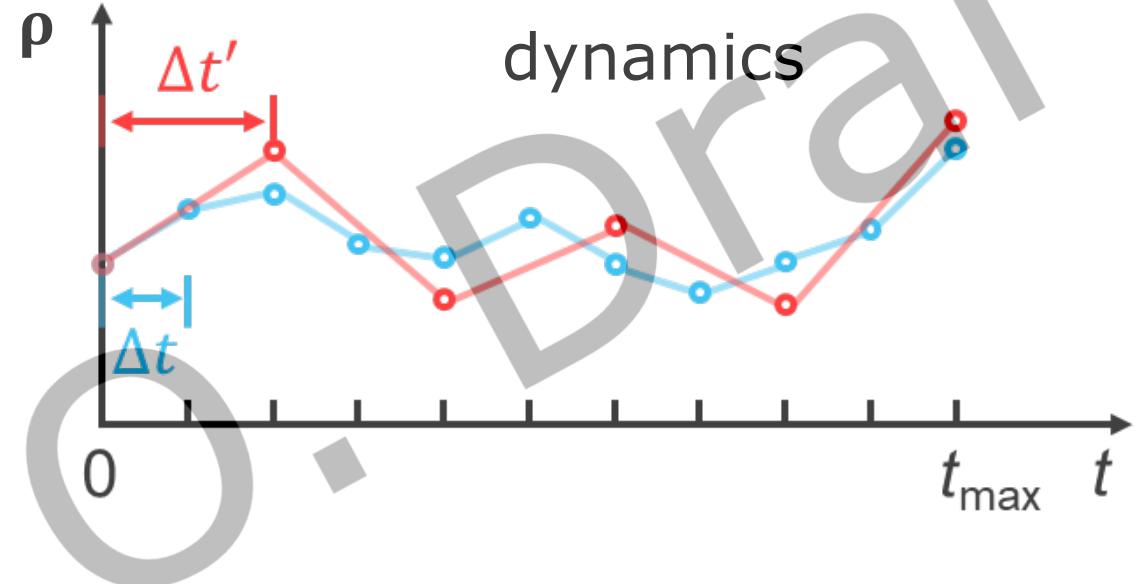
# Can we do better?

$$\rho(t) = f[\rho(t - \Delta t)]$$

dynamics propagation is

- computationally expensive
- recursive (iterative)

$$\rho(t) = f[t; \text{other parameters}]$$



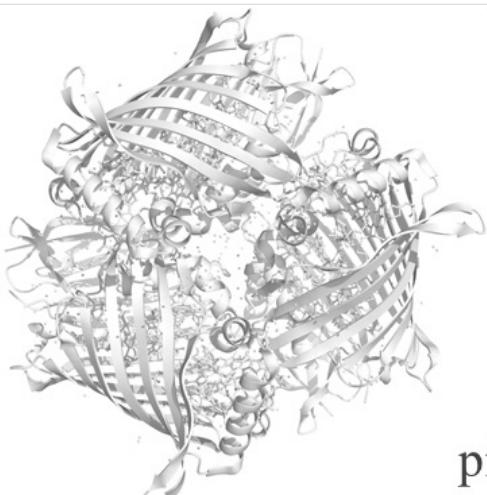
$\gamma$  = characteristic frequency

$\lambda$  = reorganization energy

$T$  = temperature

$$\rho(\text{time}) = f[\text{time}; \text{simulation parameters}]$$

PDB code: 3ENI



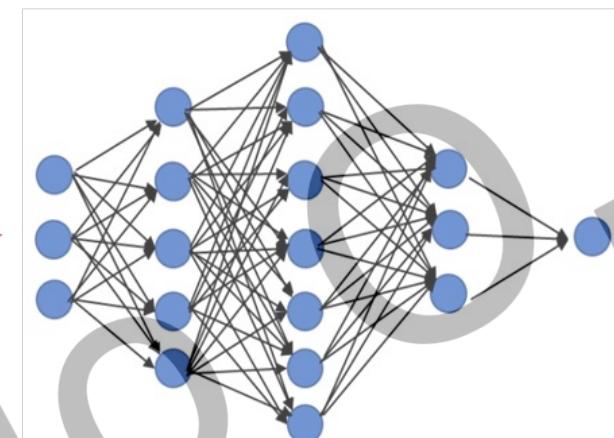
↓

$\gamma, \lambda, T$

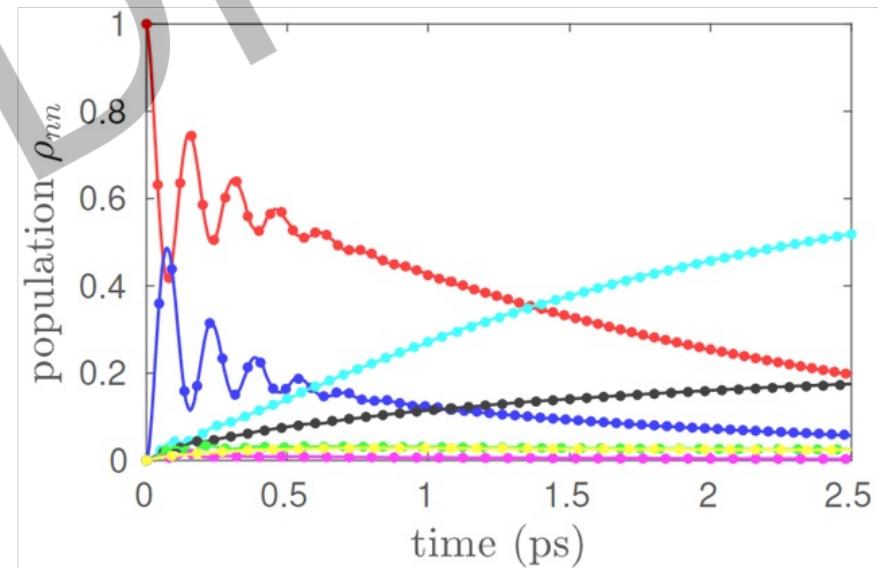


pico-second watch

2.5ps



Draft

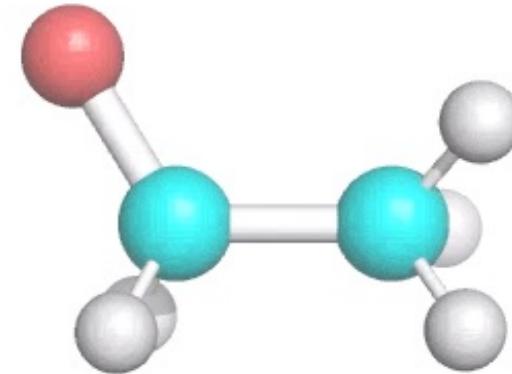


Dots: Reference  
Line: AI-QD

7-sites Fenna-Matthews-Olson (FMO) complex

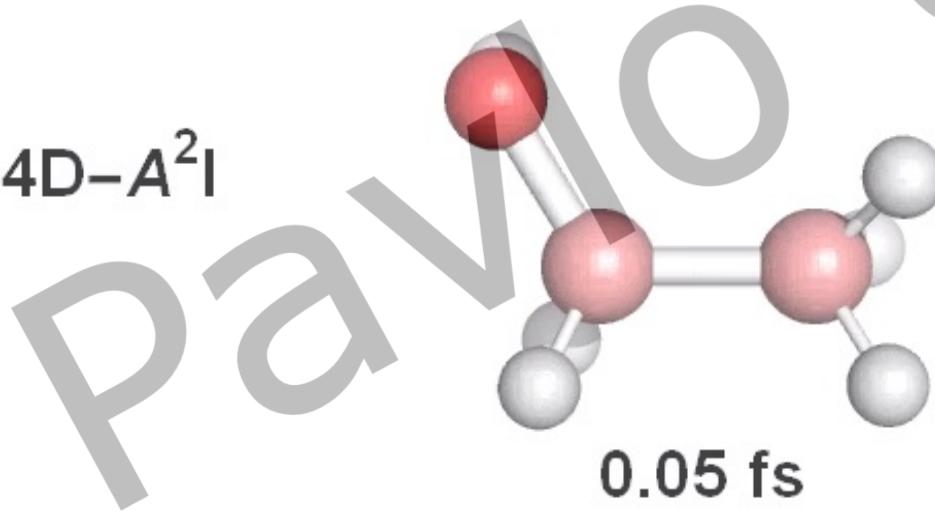
A. Ullah, P. O. Dral. Predicting the future of excitation energy transfer in light-harvesting complex with artificial intelligence-based quantum dynamics. *Nat. Commun.* **2022**, *13*, 1930

3D MD



1 CPU day per 2.5 ps

4D-A<sup>2</sup>I



0.05 fs

1 ns per 1 hour wall-clock time on  
a single RTX 3080Ti GPU card

# Can we do even better?

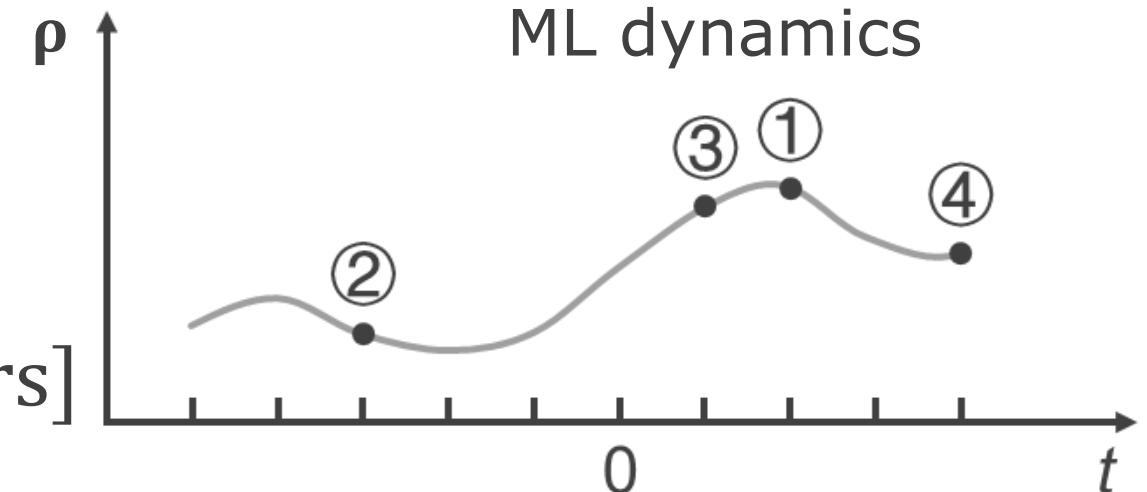
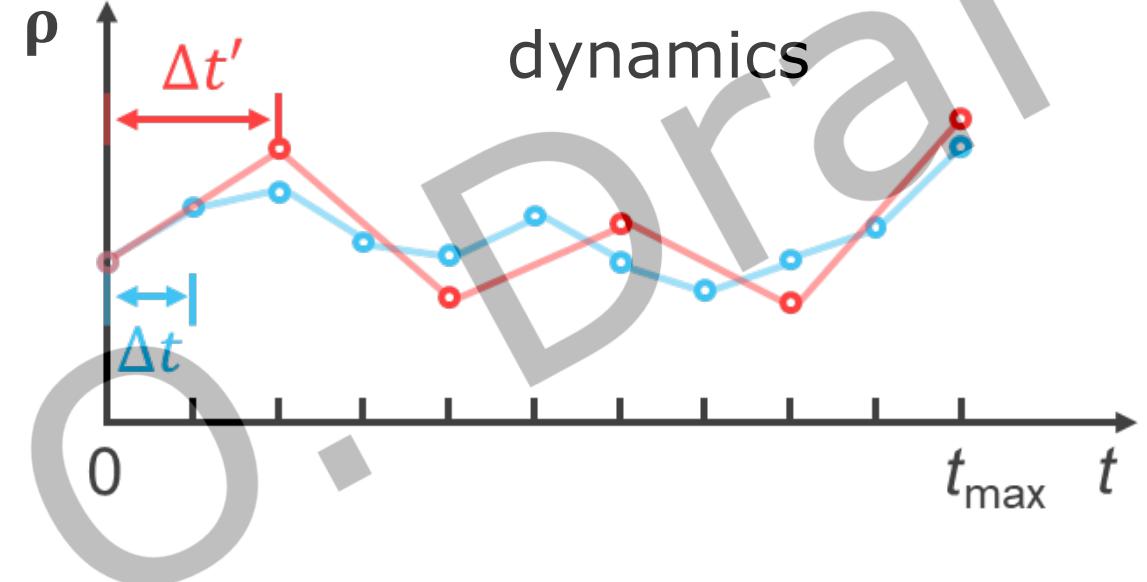
$$\rho(t) = f[\rho(t - \Delta t)]$$

dynamics propagation is

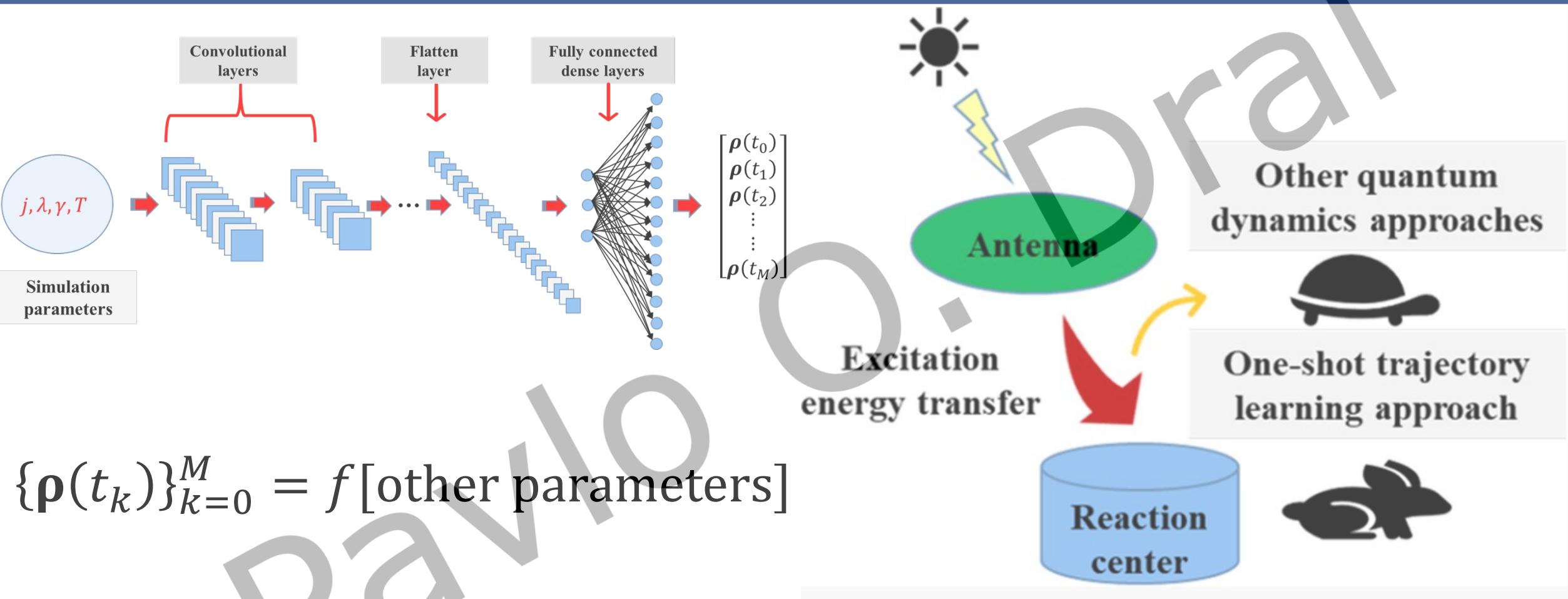
- computationally expensive
- recursive (iterative)

$$\rho(t) = f[t; \text{other parameters}]$$

$$\{\rho(t_k)\}_{k=0}^M = f[\text{other parameters}]$$



# One-Shot Trajectory Learning (OSTL)



$$\{\rho(t_k)\}_{k=0}^M = f[\text{other parameters}]$$

- **10 ps long dynamics in just 70 ms**
- good for massive simulation in parameter space

# Thank you for your attention!

Artificial intelligence in computational chemistry

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Artificial intelligence firmly entered latest advances in application of all topics include, but not limited to, machine learning, extracting chemical quantum chemical methods improve artificial intelligence methods for c

Guest editors:

**Pavlo O. Dral, PhD**

Xiamen University, Xiamen, China

(Machine learning in chemistry, Quantum chemistry, Excited states, Electronic structure simulations, Dynamics)

**Joel M. Bowman, PhD**

Emory University, Atlanta, Georgia, United States of America

(Machine learning potential energy surfaces, vibrational and reaction dynamics)

**Feliu Maseras, PhD**

Institute of Chemical Research of Catalonia, Tarragona, Spain

(Computational homogeneous catalysis; Quantum mechanics/Molecular mechanics methods; Statistical analysis of computational results)

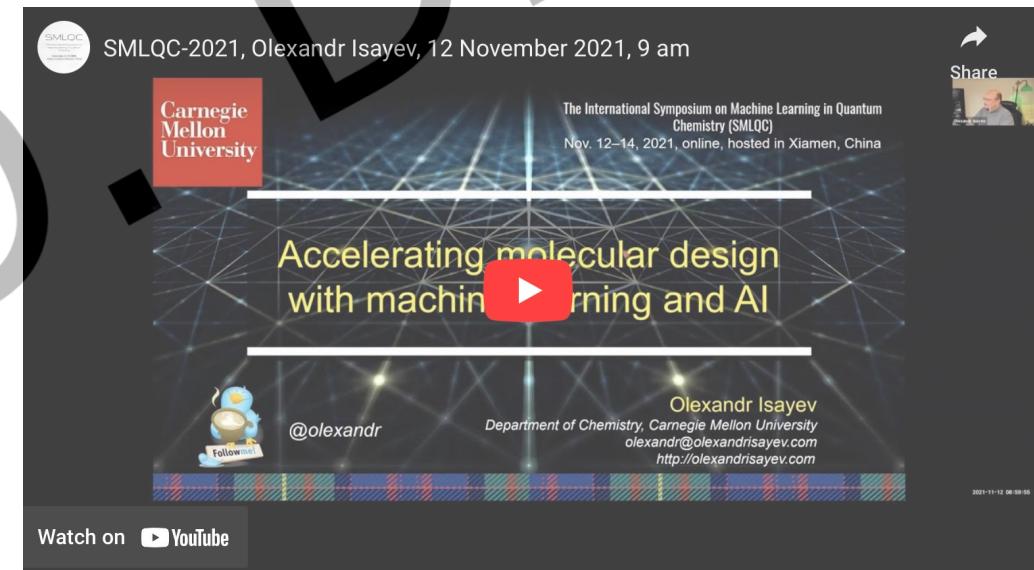
**Fang Liu, PhD**

Emory University, Atlanta, Georgia, United States of America

(quantum chemistry, solvent effects, machine learning, excited states)



**Symposia and seminars on machine learning in quantum chemistry**



**SMLQC-2023 to be held in Uppsala, Sweden  
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